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Mark Scheme (Results)

Summer 2012

GCE Core Mathematics C3
(6665) Paper 1

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Summer 2012
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Summer 2012
6665 Core Mathematics
C3 Mark Scheme

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.

2. The Edexcel Mathematics mark schemes use the following types of marks:

- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
- ft – follow through
- the symbol $\surd$ will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- ⌐ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$(x^2 + bx + c) = (x + p)(x + q),\ \text{where} \left|pq\right| = \left|c\right|$, leading to x = ...

$(ax^2 + bx + c) = (mx + p)(nx + q),\ \text{where} \left|pq\right| = \left|c\right| \text{ and } \left|mn\right| = \left|a\right|$, leading to x = …

2. Formula

Attempt to use correct formula (with values for a, b and c), leading to x = …

3. Completing the square

Solving $x^2 + bx + c = 0$: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c, \quad q \neq 0$, leading to x = …

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^n \to x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \to x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

Question Number	Scheme	Marks
1.	$9x^2-4=(3x-2)(3x+2)$ At any stage	B1
	Eliminating the common factor of $(3x+2)$ at any stage $\dfrac{2(3x+2)}{(3x-2)(3x+2)}=\dfrac{2}{3x-2}$	B1
	Use of a common denominator $\dfrac{2(3x+2)(3x+1)}{(9x^2-4)(3x+1)}-\dfrac{2(9x^2-4)}{(9x^2-4)(3x+1)}$ or $\dfrac{2(3x+1)}{(3x-2)(3x+1)}-\dfrac{2(3x-2)}{(3x+1)(3x-2)}$	M1
	$\dfrac{6}{(3x-2)(3x+1)}$ or $\dfrac{6}{9x^2-3x-2}$	A1
		(4 marks)

Notes

B1 For factorising $9x^2-4=(3x-2)(3x+2)$ using difference of two squares. It can be awarded at any stage of the answer but it must be scored on E pen as the first mark

B1 For eliminating/cancelling out a factor of $(3x+2)$ at any stage of the answer.

M1 For combining two fractions to form a single fraction with a common denominator. Allow slips on the numerator but at least one must have been adapted. Condone invisible brackets. Accept two separate fractions with the same denominator as shown in the mark scheme. Amongst possible (incorrect) options scoring method marks are

$\dfrac{2(3x+2)}{(9x^2-4)(3x+1)}-\dfrac{2(9x^2-4)}{(9x^2-4)(3x+1)}$ Only one numerator adapted, separate fractions

$\dfrac{2\times3x+1-2\times3x-2}{(3x-2)(3x+1)}$ Invisible brackets, single fraction

A1 $\dfrac{6}{(3x-2)(3x+1)}$

This is not a given answer so you can allow recovery from 'invisible' brackets.

Alternative method

$\dfrac{2(3x+2)}{(9x^2-4)}-\dfrac{2}{(3x+1)}=\dfrac{2(3x+2)(3x+1)-2(9x^2-4)}{(9x^2-4)(3x+1)}=\dfrac{18x+12}{(9x^2-4)(3x+1)}$ has scored 0,0,1,0 so far

$=\dfrac{6(3x+2)}{(3x+2)(3x-2)(3x+1)}$ is now 1,1,1,0

$=\dfrac{6}{(3x-2)(3x+1)}$ and now 1,1,1,1

Question Number	Scheme	Marks
2.	(a) $x^3+3x^2+4x-12=0 \Rightarrow x^3+3x^2=12-4x$ $\Rightarrow x^2(x+3)=12-4x$ $\Rightarrow x^2=\dfrac{12-4x}{(x+3)} \Rightarrow x=\sqrt{\dfrac{4(3-x)}{(x+3)}}$	M1 dM1A1* (3)
	(b) $x_1=1.41$, *awrt* $x_2=1.20$ $x_3=1.31$	M1A1,A1 (3)
	(c) Choosing (1.2715,1.2725) or tighter containing root 1.271998323	M1
	f(1.2725) = (+)0.00827... f(1.2715) = −0.00821....	M1
	Change of sign⇒α=1.272	A1 (3) **(9 marks)**

Notes

(a) M1 Moves from f(x)=0, which may be implied by subsequent working, to $x^2(x\pm3)=\pm12\pm4x$ by separating terms and factorising in either order. No need to factorise rhs for this mark.

dM1 Divides by '(x+3)' term to make x^2 the subject, then takes square root. No need for rhs to be factorised at this stage

A1* CSO. This is a given solution. Do not allow sloppy algebra or notation with root on just numerator for instance. The 12-4x needs to have been factorised.

(b) **Note that this appears B1,B1,B1 on EPEN**

M1 An attempt to substitute $x_0=1$ into the iterative formula to calculate x_1.

This can be awarded for the sight of $\sqrt{\dfrac{4(3-1)}{(3+1)}}$, $\sqrt{\dfrac{8}{4}}$, $\sqrt{2}$ and even 1.4

A1 $x_1=1.41$. The subscript is not important. Mark as the first value found, $\sqrt{2}$ is A0

A1 $x_2=$ awrt 1.20 $x_3=$ awrt 1.31. Mark as the second and third values found. Condone 1.2 for x_2

(c) **Note that this appears M1A1A1 on EPEN**

M1 Choosing the interval (1.2715,1.2725) or tighter containing the root 1.271998323.
Continued iteration is not allowed for this question and is M0

M1 Calculates f(1.2715) and f(1.2725), or **the** tighter interval with at least 1 correct to 1 sig fig rounded or truncated.
Accept f(1.2715) = -0.008 1sf rounded or truncated. Also accept f(1.2715) = -0.01 2dp
Accept f(1.2725) = (+)0.008 1sf rounded or truncated. Also accept f(1.2725) = (+)0.01 2dp

A1 Both values correct (see above),
A valid reason; Accept change of sign, or >0 <0, or f(1.2715) ×f(1.2725)<0
And a (minimal) conclusion; Accept hence root or α=1.272 or QED or □

Alternative to (a) working backwards

2(a)

	$x=\sqrt{\dfrac{4(3-x)}{(x+3)}} \Rightarrow x^2=\dfrac{4(3-x)}{(x+3)} \Rightarrow x^2(x+3)=4(3-x)$	M1
	$x^3+3x^2=12-4x \Rightarrow x^3+3x^2+4x-12=0$	dM1
	States that this is f(x)=0	A1* (3)

Alternative starting with the given result and working backwards

M1 Square (both sides) and multiply by (x+3)

dM1 Expand brackets and collect terms on one side of the equation =0

A1 A statement to the effect that this is f(x)=0

An acceptable answer to (c) with an example of a tighter interval

M1 Choosing the interval (1.2715, 1.2720). This contains the root 1.2719(98323)

M1 Calculates f(1.2715) and f(1.2720), with at least 1 correct to 1 sig fig rounded or truncated.
Accept f(1.2715) = -0.008 1sf rounded or truncated f(1.2715) = -0.01 2dp
Accept f(1.2720) = (+)0.00003 1sf rounded or f(1.2720) = (+)0.00002 truncated 1sf

A1 Both values correct (see above),
A valid reason; Accept change of sign, or >0 <0, or f(1.2715) ×f(1.2720)<0
And a (minimal) conclusion; Accept hence root or α=1.272 or QED or □

x	**f(*x*)**
1.2715	-0.00821362
1.2716	-0.00656564
1.2717	-0.00491752
1.2718	-0.00326927
1.2719	-0.00162088
1.2720	+0.00002765
1.2721	+0.00167631
1.2722	+0.00332511
1.2723	+0.00497405
1.2724	+0.00662312
1.2725	+0.00827233

An acceptable answer to (c) using g(x) where g(x)= $\sqrt{\dfrac{4(3-x)}{(x+3)}}-x$

2nd M1 Calculates g(1.2715) and g(1.2725), or **the** tighter interval with at least 1 correct to 1 sig fig rounded or truncated.
g(1.2715) = 0.0007559. Accept g(1.2715) = awrt (+)0.0008 1sf rounded or awrt 0.0007 truncated.
g(1.2725)=-0.00076105. Accept g(1.2725) = awrt -0.0008 1sf rounded or awrt -0.0007 truncated.

Question Number	Scheme	Marks
3.	(a) $\frac{dy}{dx} = \sqrt{3}e^{x\sqrt{3}}\sin 3x + 3e^{x\sqrt{3}}\cos 3x$	M1A1
	$\frac{dy}{dx} = 0 \qquad e^{x\sqrt{3}}(\sqrt{3}\sin 3x + 3\cos 3x) = 0$	M1
	$\tan 3x = -\sqrt{3}$	A1
	$3x = \frac{2\pi}{3} \Rightarrow x = \frac{2\pi}{9}$	M1A1
		(6)
	(b) At x=0 $\frac{dy}{dx} = 3$	B1
	Equation of normal is $-\frac{1}{3} = \frac{y-0}{x-0}$ or any equivalent $y = -\frac{1}{3}x$	M1A1
		(3) **(9 marks)**

(a) M1 Applies the product rule vu'+uv' to $e^{x\sqrt{3}}\sin 3x$. If the rule is quoted it must be correct and there must have been some attempt to differentiate both terms. If the rule is not quoted (nor implied by their working, ie. terms are written out u=…,u'=….,v=….,v'=….followed by their vu'+uv') only accept answers of the form $\frac{dy}{dx} = Ae^{x\sqrt{3}}\sin 3x + e^{x\sqrt{3}} \times \pm B\cos 3x$

A1 Correct expression for $\frac{dy}{dx} = \sqrt{3}e^{x\sqrt{3}}\sin 3x + 3e^{x\sqrt{3}}\cos 3x$

M1 Sets **their** $\frac{dy}{dx} = 0$, factorises out or divides by $e^{x\sqrt{3}}$ producing an equation in sin3x and cos3x

A1 Achieves either $\tan 3x = -\sqrt{3}$ or $\tan 3x = -\frac{3}{\sqrt{3}}$

M1 Correct order of arctan, followed by ÷3.

Accept $3x = \frac{5\pi}{3} \Rightarrow x = \frac{5\pi}{9}$ or $3x = \frac{-\pi}{3} \Rightarrow x = \frac{-\pi}{9}$ but not $x = \arctan(\frac{-\sqrt{3}}{3})$

A1 CS0 $x = \frac{2\pi}{9}$ Ignore extra solutions outside the range. Withhold mark for extra inside the range.

(b) B1 Sight of **3** for the gradient

M1 A full method for finding an equation of the normal.

Their tangent gradient m must be modified to $-\frac{1}{m}$ and used together with (0, 0).

Eg $-\frac{1}{their\ 'm'} = \frac{y-0}{x-0}$ or equivalent is acceptable

A1 $y = -\frac{1}{3}x$ or any correct equivalent including $-\frac{1}{3} = \frac{y-0}{x-0}$.

Alternative in part (a) using the form $R\sin(3x+\alpha)$ JUST LAST 3 MARKS

Question Number	Scheme	Marks
3.	(a) $\frac{dy}{dx} = \sqrt{3}e^{x\sqrt{3}}\sin 3x + 3e^{x\sqrt{3}}\cos 3x$	M1A1
	$\frac{dy}{dx} = 0 \qquad e^{x\sqrt{3}}(\sqrt{3}\sin 3x + 3\cos 3x) = 0$	M1
	$(\sqrt{12})\sin(3x+\frac{\pi}{3}) = 0$	A1
	$3x = \frac{2\pi}{3} \Rightarrow x = \frac{2\pi}{9}$	M1A1
		(6)

A1 Achieves either $(\sqrt{12})\sin(3x+\frac{\pi}{3}) = 0$ or $(\sqrt{12})\cos(3x-\frac{\pi}{6}) = 0$

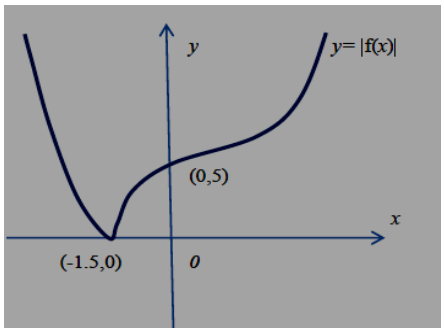
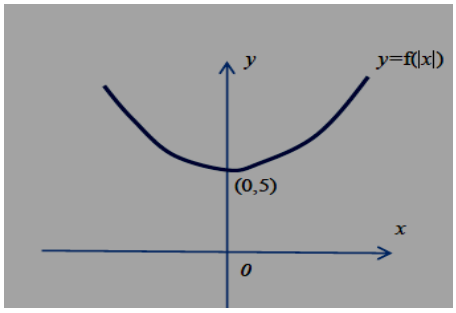
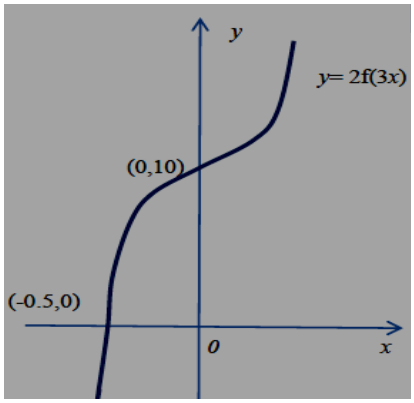
M1 Correct order of arcsin or arcos, etc to produce a value of x

Eg accept $3x+\frac{\pi}{3} = 0$ or π or $2\pi \Rightarrow x = ...$

A1 Cao $x = \frac{2\pi}{9}$ Ignore extra solutions outside the range. Withhold mark for extra inside the range.

Alternative to part (a) squaring both sides JUST LAST 3 MARKS

Question Number	Scheme	Marks
3.	(a) $\frac{dy}{dx} = \sqrt{3}e^{x\sqrt{3}}\sin 3x + 3e^{x\sqrt{3}}\cos 3x$	M1A1
	$\frac{dy}{dx} = 0 \qquad e^{x\sqrt{3}}(\sqrt{3}\sin 3x + 3\cos 3x) = 0$	M1
	$\sqrt{3}\sin 3x = -3\cos 3x \Rightarrow \cos^2(3x) = \frac{1}{4}$ or $\sin^2(3x) = \frac{3}{4}$	A1
	$x = \frac{1}{3}\arccos(\pm\sqrt{\frac{1}{4}})$ oe	M1
	$x = \frac{2\pi}{9}$	A1

Question Number	Scheme	Marks
4.(a)	 Shape including cusp (-1.5, 0) **and** (0, 5)	B1 B1 (2)
(b)	 Shape (0,5)	B1 B1 (2)
(c)	 Shape (0,10) (-0.5, 0)	B1 B1 B1 (3) **(7 marks)**

(a) **Note that this appears as M1A1 on EPEN**

B1 Shape (inc cusp) with graph in just quadrants 1 and 2. Do not be overly concerned about relative gradients, but the left hand section of the curve should not bend back beyond the cusp

B1 This is independent, and for the curve touching the x-axis at (-1.5, 0) **and** crossing the y-axis at (0,5)

(b) **Note that this appears as M1A1 on EPEN**

B1 For a U shaped curve symmetrical about the y- axis

B1 (0,5) lies on the curve

(c) **Note that this appears as M1B1B1 on EPEN**

B1 Correct shape- do not be overly concerned about relative gradients. Look for a similar shape to f(x)

B1 Curve **crosses** the y axis at (0, 10). The curve must appear in both quadrants 1 and 2

B1 Curve **crosses** the x axis at (-0.5, 0). The curve must appear in quadrants 3 and 2.

In all parts accept the following for any co-ordinate. Using (0,3) as an example, accept both (3,0) or 3 written on the y axis (as long as the curve passes through the point)

Special case with (a) and (b) completely correct but the wrong way around mark - SC(a) 0,1 SC(b) 0,1
Otherwise follow scheme

Question Number	Scheme	Marks
5.	(a) $4\operatorname{cosec}^2 2\theta - \operatorname{cosec}^2\theta = \dfrac{4}{\sin^2 2\theta} - \dfrac{1}{\sin^2\theta}$	
	$= \dfrac{4}{(2\sin\theta\cos\theta)^2} - \dfrac{1}{\sin^2\theta}$	B1 B1
		(2)
	(b) $\dfrac{4}{(2\sin\theta\cos\theta)^2} - \dfrac{1}{\sin^2\theta} = \dfrac{4}{4\sin^2\theta\cos^2\theta} - \dfrac{1}{\sin^2\theta}$	
	$= \dfrac{1}{\sin^2\theta\cos^2\theta} - \dfrac{\cos^2\theta}{\sin^2\theta\cos^2\theta}$	M1
	Using $1-\cos^2\theta = \sin^2\theta$ $= \dfrac{\sin^2\theta}{\sin^2\theta\cos^2\theta}$	M1
	$= \dfrac{1}{\cos^2\theta} = \sec^2\theta$	M1A1*
		(4)
	(c) $\sec^2\theta = 4 \Rightarrow \sec\theta = \pm 2 \Rightarrow \cos\theta = \pm\dfrac{1}{2}$	M1
	$\theta = \dfrac{\pi}{3}, \dfrac{2\pi}{3}$	A1,A1
		(3)
		(9 marks)

Note (a) and (b) can be scored together

(a) B1 One term correct. Eg. writes $4\operatorname{cosec}^2 2\theta$ as $\dfrac{4}{(2\sin\theta\cos\theta)^2}$ **or** $\operatorname{cosec}^2\theta$ as $\dfrac{1}{\sin^2\theta}$. Accept terms like $\operatorname{cosec}^2\theta = 1+\cot^2\theta = 1+\dfrac{\cos^2\theta}{\sin^2\theta}$. The question merely asks for an expression in sin θ and cos θ

B1 A fully correct expression in sin θ and cos θ . Eg. $\dfrac{4}{(2\sin\theta\cos\theta)^2} - \dfrac{1}{\sin^2\theta}$ **Accept equivalents**

Allow a different variable say x's instead of θ's but do not allow mixed units.

b) M1 Attempts to combine their expression in $\sin\theta$ and $\cos\theta$ using a common denominator. The terms can be separate but the denominator must be correct and one of the numerators must have been adapted

M1 Attempts to form a 'single' term on the numerator by using the identity $1-\cos^2\theta = \sin^2\theta$

M1 Cancels correctly by $\sin^2\theta$ terms and replaces $\dfrac{1}{\cos^2\theta}$ with $\sec^2\theta$

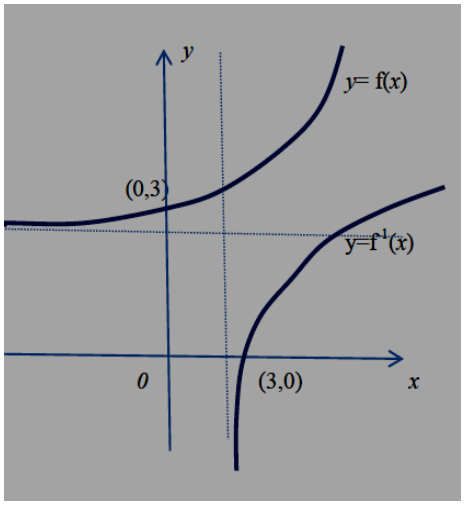
A1* Cso. This is a given answer. All aspects must be correct

IF IN ANY DOUBT SEND TO REVIEW OR CONSULT YOUR TEAM LEADER

c) M1 For $\sec^2\theta = 4$ leading to a solution of $\cos\theta$ by taking the root and inverting in either order . Similarly accept $\tan^2\theta = 3, \sin^2\theta = \dfrac{3}{4}$ leading to solutions of $\tan\theta, \sin\theta$. Also accept $\cos 2\theta = -\dfrac{1}{2}$

A1 Obtains one correct answer usually $\theta = \dfrac{\pi}{3}$ Do not accept decimal answers or degrees

A1 Obtains both correct answers. $\theta = \dfrac{\pi}{3}, \dfrac{2\pi}{3}$ Do not award if there are extra solutions inside the range. Ignore solutions outside the range.

Question Number	Scheme	Marks
6.	(a) f(x)>2	B1 (1)
	(b) $fg(x) = e^{\ln x} + 2, = x + 2$	M1,A1 (2)
	(c) $e^{2x+3} + 2 = 6 \Rightarrow e^{2x+3} = 4$ $\Rightarrow 2x + 3 = \ln 4$ $\Rightarrow x = \frac{\ln 4 - 3}{2}$ or ln2-$\frac{3}{2}$	M1A1 M1A1 (4)
	(d) Let $y = e^x + 2 \Rightarrow y - 2 = e^x \Rightarrow \ln(y-2) = x$ $f^{-1}(x) = \ln(x-2), \quad x > 2.$	M1 A1 , **B1ft** (3)
	(e)  Shape for f(x) B1 (0, 3) B1 Shape for f^{-1}(x) B1 (3, 0) B1	(4)
		(14 marks)

(a) B1 Range of f(x)>2. Accept y>2, (2,∞), f>2, as well as 'range is the set of numbers bigger than 2' but **don't accept** x>2

(b) M1 For applying the correct order of operations. Look for $e^{\ln x} + 2$. Note that $\ln e^x + 2$ is M0

A1 Simplifies $e^{\ln x} + 2$ to $x + 2$. Just the answer is acceptable for both marks

(c) M1 Starts with $e^{2x+3} + 2 = 6$ and proceeds to $e^{2x+3} = ...$

A1 $e^{2x+3} = 4$

M1 Takes ln's both sides, $2x + 3 = \ln..$ and proceeds to x=….

A1 $x = \frac{\ln 4 - 3}{2}$ oe. eg ln2 - $\frac{3}{2}$ Remember to isw any incorrect working after a correct answer

(d) **Note that this is marked M1A1A1 on EPEN**

M1 Starts with $y = e^x + 2$ or $x = e^y + 2$ and attempts to change the subject.
All ln work must be correct. The 2 must be dealt with first.
Eg. $y = e^x + 2 \Rightarrow \ln y = x + \ln 2 \Rightarrow x = \ln y - \ln 2$ is M0

A1 $f^{-1}(x) = \ln(x-2)$ or $y = \ln(x-2)$ or $y = \ln|x-2|$ There must be some form of bracket

B1ft Either $x>2$, or follow through on their answer to part (a), provided that it wasn't $y \in \Re$
Do not accept $y>2$ or $f^{-1}(x)>2$.

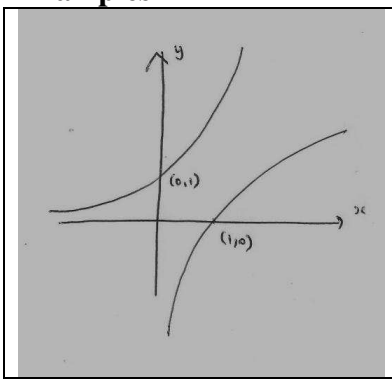
(e) B1 Shape for $y=e^x$. The graph should only lie in quadrants 1 and 2. It should start out with a gradient that is approx. 0 above the x axis in quadrant 2 and increase in gradient as it moves into quadrant 1. You should not see a minimum point on the graph.

B1 (0, 3) lies on the curve. Accept 3 written on the y axis as long as the point lies on the curve

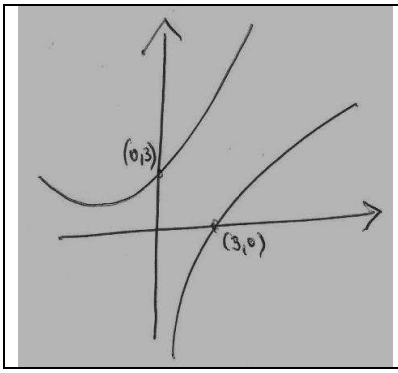
B1 Shape for $y=\ln x$. The graph should only lie in quadrants 4 and 1. It should start out with gradient that is approx. infinite to the right of the y axis in quadrant 4 and decrease in gradient as it moves into quadrant 1. You should not see a maximum point. Also with hold this mark if it intersects $y=e^x$

B1 (3, 0) lies on the curve. Accept 3 written on the x axis as long as the point lies on the curve

Condone lack of labels in this part
Examples



Scores **1,0,1,0.**
Both shapes are fine, do not be concerned about asymptotes appearing at x=2, y=2. (See notes)
Both co-ordinates are incorrect



Scores **0,1,1,1**
Shape for $y = e^x$ is incorrect, there is a minimum point on the graph.
All other marks an be awarded

Question Number	Scheme	Marks
7.	(a)(i) $\dfrac{\mathrm{d}}{\mathrm{d}x}(\ln(3x)) = \dfrac{3}{3x}$	M1
	$\dfrac{\mathrm{d}}{\mathrm{d}x}(x^{\frac{1}{2}}\ln(3x)) = \ln(3x)\times\dfrac{1}{2}x^{-\frac{1}{2}} + x^{\frac{1}{2}}\times\dfrac{3}{3x}$	M1A1
		(3)
	(ii) $\dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{(2x-1)^5\times -10-(1-10x)\times 5(2x-1)^4\times 2}{(2x-1)^{10}}$	M1A1
	$\dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{80x}{(2x-1)^6}$	A1
		(3)
	(b) $x = 3\tan 2y \Rightarrow \dfrac{\mathrm{d}x}{\mathrm{d}y} = 6\sec^2 2y$	M1A1
	$\Rightarrow \dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{1}{6\sec^2 2y}$	M1
	Uses $\sec^2 2y = 1+\tan^2 2y$ and uses $\tan 2y = \dfrac{x}{3}$	
	$\Rightarrow \dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{1}{6(1+(\frac{x}{3})^2)} = (\dfrac{3}{18+2x^2})$	M1A1
		(5) **(11 marks)**

Note that this is marked B1M1A1 on EPEN

(a)(i) M1 Attempts to differentiate $\ln(3x)$ to $\dfrac{B}{x}$. Note that $\dfrac{1}{3x}$ is fine.

M1 Attempts the product rule for $x^{\frac{1}{2}}\ln(3x)$. If the rule is quoted it must be correct. There must have been some attempt to differentiate both terms.
If the rule is not quoted nor implied from their stating of u, u', v, v' and their subsequent expression, only accept answers of the form

$\ln(3x)\times Ax^{-\frac{1}{2}} + x^{\frac{1}{2}}\times\dfrac{B}{x}, \quad A, B > 0$

A1 Any correct (un simplified) form of the answer. Remember to isw any incorrect further work

$\dfrac{d}{dx}(x^{\frac{1}{2}}\ln(3x)) = \ln(3x)\times\dfrac{1}{2}x^{-\frac{1}{2}} + x^{\frac{1}{2}}\times\dfrac{3}{3x} = (\dfrac{\ln(3x)}{2\sqrt{x}} + \dfrac{1}{\sqrt{x}}) = x^{-\frac{1}{2}}(\dfrac{1}{2}\ln 3x + 1)$

Note that this part does not require the answer to be in its simplest form

(ii) M1 Applies the quotient rule, a version of which appears in the formula booklet. If the formula is quoted it must be correct. There must have been an attempt to differentiate both terms. If the formula is not quoted nor implied from their stating of u, u', v, v' and their subsequent expression, only accept answers of the form

$$\frac{(2x-1)^5\times\pm10-(1-10x)\times C(2x-1)^4}{(2x-1)^{10\text{ or }7\text{ or }25}}$$

A1 Any un simplified form of the answer. Eg $\frac{dy}{dx}=\frac{(2x-1)^5\times-10-(1-10x)\times5(2x-1)^4\times2}{((2x-1)^5)^2}$

A1 Cao. It must be simplified as required in the question $\frac{dy}{dx}=\frac{80x}{(2x-1)^6}$

(b) M1 Knows that $3\tan 2y$ differentiates to $C\sec^2 2y$. The lhs can be ignored for this mark. If they write $3\tan 2y$ as $\frac{3\sin 2y}{\cos 2y}$ this mark is awarded for a correct attempt of the quotient rule.

A1 Writes down $\frac{dx}{dy}=6\sec^2 2y$ or implicitly to get $1=6\sec^2 2y\frac{dy}{dx}$

Accept from the quotient rule $\frac{6}{\cos^2 2y}$ or even $\frac{\cos 2y\times6\cos 2y-3\sin 2y\times-2\sin 2y}{\cos^2 2y}$

M1 An attempt to invert 'their' $\frac{dx}{dy}$ to reach $\frac{dy}{dx}=f(y)$, or changes the subject of their implicit

. differential to achieve a similar result $\frac{dy}{dx}=f(y)$

M1 Replaces an expression for $\sec^2 2y$ in their $\frac{dx}{dy}$ or $\frac{dy}{dx}$ with x by attempting to use

$\sec^2 2y=1+\tan^2 2y$. Alternatively, replaces an expression for y in $\frac{dx}{dy}$ or $\frac{dy}{dx}$ with $\frac{1}{2}\arctan(\frac{x}{3})$

A1 Any correct form of $\frac{dy}{dx}$ in terms of x. $\frac{dy}{dx}=\frac{1}{6(1+(\frac{x}{3})^2)}$ $\frac{dy}{dx}=\frac{3}{18+2x^2}$ *or* $\frac{1}{6\sec^2(\arctan(\frac{x}{3}))}$

Question Number	Scheme	Marks
7.	**(a)(ii) Alt using the product rule**	
	Writes $\frac{1-10x}{(2x-1)^5}$ as $(1-10x)(2x-1)^{-5}$ and applies vu'+uv'.	
	See (a)(i) for rules on how to apply	
	$(2x-1)^{-5}\times-10+(1-10x)\times-5(2x-1)^{-6}\times2$	M1A1
	Simplifies as main scheme to $80x(2x-1)^{-6}$ or equivalent	A1
		(3)
	(b) Alternative using arctan. They must attempt to differentiate to score any marks. Technically this is M1A1M1A2	
	Rearrange $x=3\tan 2y$ to $y=\frac{1}{2}\arctan(\frac{x}{3})$ **and attempt to differentiate**	M1A1
	Differentiates to a form $\frac{A}{1+(\frac{x}{3})^2}$, $=\frac{1}{2}\times\frac{1}{(1+(\frac{x}{3})^2)}\times\frac{1}{3}$ or $\frac{1}{6(1+(\frac{x}{3})^2)}$ oe	M1, A2
		(5)

Question Number	Scheme	Marks
8.	(a) $R=25$	B1
	$\tan\alpha = \frac{24}{7} \Rightarrow \alpha = (\text{awrt})73.7^0$	M1A1
		(3)
	(b) $\cos(2x + their\,\alpha) = \frac{12.5}{their\ R}$	M1
	$2x + their'\alpha' = 60^0$	A1
	$2x + their'\alpha' =$ their 300^0 or their $420^0 \Rightarrow x = ..$	M1
	$x = awrt\ 113.1^0, 173.1^0$	A1A1
		(5)
	(c) Attempts to use $\cos 2x = 2\cos^2 x - 1$ **AND** $\sin 2x = 2\sin x\cos x$ in the expression	M1
	$14\cos^2 x - 48\sin x\cos x = 7(\cos 2x + 1) - 24\sin 2x$	
	$= 7\cos 2x - 24\sin 2x + 7$	A1
		(2)
	(d) $14\cos^2 x - 48\sin x\cos x = R\cos(2x + \alpha) + 7$	
	Maximum value ='R'+'c'	M1
	= 32 cao	A1
		(2)
		(12 marks)

(a) B1 Accept 25, awrt 25.0, √625. Condone ±25

M1 For $\tan\alpha = \pm\frac{24}{7}$ $\tan\alpha = \pm\frac{7}{24}$ $\sin\alpha = \pm\frac{24}{their\ R}$, $\cos\alpha = \pm\frac{7}{their\ R}$

A1 $\alpha = (\text{awrt})73.7^0$. The answer 1.287 (radians) is A0

(b) M1 For using part (a) and dividing by their R to reach $\cos(2x + their\,\alpha) = \frac{12.5}{their\ R}$

A1 Achieving $2x + their\ \alpha = 60^{(0)}$. This can be implied by $113.1^{(0)}/113.2^{(0)}$ or $173.1^{(0)}/173.2^{(0)}$ or $-6.8^{(0)}/-6.85^{(0)}/-6.9^{(0)}$

M1 Finding a secondary value of x from their principal value. A correct answer will imply this mark
Look for $\frac{360 \pm \text{'their' principal value} \pm \text{'their'}\,\alpha}{2}$

A1 $x = awrt\ 113.1^0/113.2^0$ OR $173.1^0/173.2^0$.

A1 $x = awrt\ 113.1^0$ AND 173.1^0. Ignore solutions outside of range. Penalise this mark for extra solutions inside the range

(c) M1 Attempts to use $\cos 2x = 2\cos^2 x - 1$ **and** $\sin 2x = 2\sin x \cos x$ in expression.
Allow slips in sign on the $\cos 2x$ term. So accept $2\cos^2 x = \pm\cos 2x \pm 1$

A1 Cao $= 7\cos 2x - 24\sin 2x + 7$. The order of terms is not important. Also accept a=7, b=-24, c=7

(d) M1 This mark is scored for adding their *R* to their *c*

A1 cao 32

Radian solutions- they will lose the first time it occurs (usually in a with 1.287 radians) Part b will then be marked as follows

(b) M1 For using part (a) and dividing by their *R* to reach $\cos(2x + their\,\alpha) = \dfrac{12.5}{their\ R}$

A1 The correct principal value of $\dfrac{\pi}{3}$ or awrt 1.05 radians. Accept $60^{(0)}$

This can be implied by awrt – 0.12 radians or awrt or 1.97 radians or awrt 3.02 radians

M1 Finding a secondary value of *x* from their principal value. A correct answer will imply this mark

Look for $\dfrac{2\pi \pm \text{'their' principal value} \pm \text{'their'}\,\alpha}{2}$ Do not allow mixed units.

A1 $x = awrt\ 1.97$ OR 3.02.

A1 $x = awrt\ 1.97$ AND 3.02. Ignore solutions outside of range. Penalise this mark for extra solutions inside the range

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